

An Approach for the Stone–Céché Type Compactifications of Plain Texture Spaces

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Abstract

In this study, the authors present an approach for the construction of a Stone–Céché type compactification of plain ditopological texture spaces in terms of difunctions.

Mathematics Subject Classification: 54E55

Keywords: Texturing, plain texture space, ditopology, evaluation difunction, dcompactness, Tychonoff dicube

1 Introduction

A texturing on a set S is a point separating, complete, completely distributive lattice \mathcal{S} of subsets of S with respect to inclusion which contains S, \emptyset and, for which arbitrary meet coincides with intersection and finite joins coincide with union. Then (S, \mathcal{S}) is called a texture space. For $s \in S$ the set P_s is defined by $P_s = \bigcap \{A \mid s \in A \in \mathcal{S}\}$. Dually we define the set $Q_s \in \mathcal{S}$ by $Q_s = \bigvee \{P_t \mid s \notin P_t\}$ for every $s \in S$. (S, \mathcal{S}) is called *plain* if arbitrary join coincides with union, namely $P_s \not\subseteq Q_s$ for every $s \in S$ [3]. Let (f, F) be a

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direlation [5] from (S, \mathcal{S}) to (T, \mathcal{T}) . Then (f, F) is called a *difunction* from (S, \mathcal{S}) to (T, \mathcal{T}) if

1. for $s, s' \in S$, $P_s \not\subseteq Q_{s'} \Rightarrow \exists t \in T$ with $f \not\subseteq \overline{Q}_{(s,t)}$ and $\overline{P}_{(s',t)} \not\subseteq F$.
2. for $t, t' \in T$ and $s \in S$, $f \not\subseteq \overline{Q}_{(s,t)}$ and $\overline{P}_{(s,t')} \not\subseteq F \Rightarrow P_{t'} \not\subseteq Q_t$.

It is known that difunctions and textures form a category which is denoted by **dfTex** [5]. A *ditopology* [3] on a texture space (S, \mathcal{S}) is a pair (τ, κ) of subsets of \mathcal{S} , where the family of *open sets* τ satisfies

- (i) $S, \emptyset \in \tau$,
- (ii) $G_1, G_2 \in \tau \Rightarrow G_1 \cap G_2 \in \tau$ and
- (iii) $G_i \in \tau, i \in I \Rightarrow \bigvee_i G_i \in \tau$,

and the family of *closed sets* κ satisfies

- (i) $S, \emptyset \in \kappa$,
- (ii) $K_1, K_2 \in \kappa \Rightarrow K_1 \cup K_2 \in \kappa$ and
- (iii) $K_i \in \kappa, i \in I \Rightarrow \bigcap K_i \in \kappa$.

Let $A \subseteq S$. Then we define

$$[A]^\kappa = \bigcap \{F \mid A \subseteq F, F \in \kappa\} (\kappa - \text{closure})$$

and

$$]A[^\tau = \bigvee \{G \mid G \subseteq A, G \in \tau\} (\tau - \text{interior}).$$

Definition 1.1 [2] Let $(S, \mathcal{S}, \tau, \kappa)$ and (T, \mathcal{T}, u, v) be ditopological texture spaces and (f, F) be a difunction from S to T . Then (f, F) is called a *diembedding* from S to T if there exists a bidense ditopological principle subtexture $(N, \mathcal{T}_N, u_N, v_N)$ of (T, \mathcal{T}, u, v) such that $(f_{S \times N}, F_{S \times N}) : (S, \mathcal{S}) \rightarrow (N, \mathcal{T}_N)$ is a dihomeomorphism. If (T, \mathcal{T}, u, v) is dicompact, then $((f, F), (T, \mathcal{T}, u, v))$ is called a *dicompactification* of (S, \mathcal{S}) .

Lemma 1.2 [5] Let $(S, \mathcal{S}), (T, \mathcal{T})$ be textures and $\psi : S \rightarrow T$ be point function satisfying the following conditions:

- (a) $s, s' \in S, P_s \not\subseteq Q_{s'} \Rightarrow P_{\psi(s)} \not\subseteq Q_{\psi(s')}$.
- (b) $P_{\psi(s)} \not\subseteq B, B \in \tau \Rightarrow \exists s' \in S$ with $P_s \not\subseteq Q_{s'}$ for which $P_{\psi(s')} \not\subseteq B$.

- (c) For $A \in \tau$ and $s \in S^b$ we have $A \not\subseteq Q_{\psi(s)} \Rightarrow A \not\subseteq Q_{\psi(u)}$ for some $P_u \not\subseteq Q_s$.

Then the difunction (f_ψ, F_ψ) corresponding to ψ satisfies the equalities

$$f_\psi = \bigvee \{\overline{P}_{(s, \psi(s))} \mid s \in S\} \text{ and } G_\psi = \bigcap \{\overline{Q}_{(s, \psi(s))} \mid s \in S\}.$$

Further, $f_\psi^- A = F_\psi^- A = \psi^{-1}(A)$ for all $A \in \mathcal{T}$.

If we take the textures in Lemma 1.2 as plain textures, then any point function satisfies the conditions (b) and (c). As a result, we may say that plain textures and the point functions satisfying (a), form a category which is denoted by **fPTex**. Further, the category of ditopological plain texture spaces and continuous point functions is denoted by **fPDitop** [5].

Definition 1.3 [1] A ditopological texture space $(S, \mathcal{S}, \tau, \kappa) \in \text{Ob fPDitop}$ is called

- (i) *completely regular* if given $G \in \tau, G \not\subseteq Q_s$, there exists a bicontinuous function $\psi : S \rightarrow \mathbb{I}$ satisfying $\psi(P_s) = \{0\}$ and $\psi(S \setminus G) = \{1\}$.
- (ii) *completely co-regular* if given $K \in \kappa, P_s \not\subseteq K$, there exists a bicontinuous function $\psi : S \rightarrow \mathbb{I}$ satisfying $\psi(S \setminus Q_s) = \{1\}$ and $\psi(K) = \{0\}$.
- (iii) *completely biregular* if it is completely regular and completely co-regular.

Recall that the category of plain ditopological texture spaces and bicontinuous difunctions is denoted by **dfPDitop** [6].

Theorem 1.4 [1] $(S, \mathcal{S}, \tau, \kappa)$ is completely biregular in **fPDitop** if and only if it is completely biregular in **dfPDitop**.

Theorem 1.5 [3] If a ditopological texture space $(S, \mathcal{S}, \tau, \kappa)$ is $\text{bi-}T_{3\frac{1}{2}}$, then there exists a bicontinuous and injective difunction from S to the Tychonoff dicube.

For more details and the concepts which are not explained here, the reader is due to [4-8].

2 The Stone–Céch Compactification

Theorem 2.1 *Let $\psi \in \text{Mor fPTex}$ and $\psi(S) \in \mathcal{T}$. Then*

- (i) $f_{\psi}^{\rightarrow} S = \psi(S)$.
- (ii) $((f_{\psi})_{S \times \psi(S)}, (F_{\psi})_{S \times \psi(S)})$ is surjective.

Proof (i) Suppose that $f_{\psi}^{\rightarrow} S \not\subseteq Q_t$ for some $t \in T$. Then $f_{\psi} \not\subseteq \overline{Q}_{(s,t)}$ and $S \not\subseteq Q_s$ for some $s \in S$. Hence, there exists a point $s' \in S$ such that $\overline{P}_{(s',\psi(s'))} \not\subseteq \overline{Q}_{(s,t)}$ and so $P_{\psi(s)} \not\subseteq Q_t$. Since $P_t \subseteq P_{\psi(s)}$, then $t \in \psi(S)$, that is $f_{\psi}^{\rightarrow} S \subseteq \psi(S)$. Now assume that $\psi(S) \not\subseteq f_{\psi}^{\rightarrow} S$. Choose a point $t \in T$ where $t \in \psi(S)$ and $t \notin f_{\psi}^{\rightarrow} S$. Then there exists a point $t' \in T$ such that $P_t \not\subseteq Q_{t'}$ and for all $s \in S$,

$$f_{\psi} \not\subseteq \overline{Q}_{(s,t')} \Rightarrow S \subseteq Q_s.$$

Since there is a point $s' \in S$ with $\psi(s') = t$, then $P_{\psi(s')} \not\subseteq Q_{t'}$ and so $\overline{P}_{(s',\psi(s'))} \not\subseteq \overline{Q}_{(s',t')}$. Therefore, $f_{\psi} \not\subseteq \overline{Q}_{(s',t')}$ and this gives $S \subseteq Q_{s'}$. Since (S, \mathcal{S}) is plain, then $P_{s'} \not\subseteq Q_{s'}$ is a contradiction. As a result, $\psi(S) \subseteq f_{\psi}^{\rightarrow} S$ and this complete the proof of (i).

(ii) Let $P_t \not\subseteq Q_{t'}$ and $t, t' \in \psi(S)$. Let us choose a point $w \in \psi(S)$ where $P_t \not\subseteq Q_w$ and $P_w \not\subseteq Q_{t'}$. Take $s \in S$ with $\psi(s) = w$. Then $P_{\psi(s)} \not\subseteq Q_{t'} \Rightarrow \overline{P}_{(s,\psi(s))} \not\subseteq \overline{Q}_{(s,t')} \Rightarrow f_{\psi} \not\subseteq \overline{Q}_{(s,t')} \Rightarrow f_{\psi} \cap (S \times \psi(S)) \not\subseteq \overline{Q}_{(s,t')} \Rightarrow (f_{\psi})_{S \times \psi(S)} \not\subseteq \overline{Q}_{(s,t')}$. Further, $P_t \not\subseteq Q_{\psi(s)} \Rightarrow P_{(s,t)} \not\subseteq Q_{(s,\psi(s))} \Rightarrow P_{(s,t)} \not\subseteq F_{\psi} \Rightarrow P_{(s,t)} \not\subseteq F_{\psi} \cap (S \times B) \Rightarrow P_{(s,t)} \not\subseteq (F_{\psi})_{(S \times \psi(S))}$.

Definition 2.2 *Let $(S, \mathcal{S}), (S_{\alpha}, \mathcal{S}_{\alpha}) \in \text{Ob fPTex}$ and $\varphi_{\alpha} \in \text{Mor fPTex}$ (S, S_{α}) for $\alpha \in J$. Then the function $\varepsilon : S \rightarrow \prod_{\alpha \in J} S_{\alpha}$ defined by*

$$\varepsilon(s) = (\varphi_{\alpha}(s))_{\alpha \in J}$$

is called an evaluation function.

Theorem 2.3 $\varepsilon \in \text{Mor fPTex}$.

Proof Clearly for each $\alpha \in J$, $\rho_{\alpha} \circ \varepsilon = \varphi_{\alpha}$ where $\rho_{\alpha} : \prod_{\alpha \in J} S_{\alpha} \rightarrow S_{\alpha}$ is the projection function. Further, by [5, Lemma 3.9] we have $\rho_{\alpha} \in \text{Mor fPTex}$. Now we show that ε satisfies (a). Let $P_s \not\subseteq Q_{s'}$ where $s, s' \in S$. Then $P_{\varphi_{\alpha}(s)} \not\subseteq Q_{\varphi_{\alpha}(s')}$ for all $\alpha \in J$ and so $P_{(\rho_{\alpha} \circ \varepsilon)(s)} \not\subseteq Q_{(\rho_{\alpha} \circ \varepsilon)(s')}$, that is $P_{\rho_{\alpha}(\varepsilon(s))} \not\subseteq Q_{\rho_{\alpha}(\varepsilon(s'))}$ for all $\alpha \in J$ and therefore, $P_{\varepsilon(s)} \not\subseteq Q_{\varepsilon(s')}$.

By Lemma 1.2 and Theorem 2.1, we have the following result:

Corollary 2.4 $(e_\varepsilon, E_\varepsilon)$ is a difunction where

$$e_\varepsilon = \bigvee \{ \overline{P}_{(s, \varepsilon(s))} \mid s \in S \} \text{ and } E_\varepsilon = \bigcap \{ \overline{Q}_{(s, \varepsilon(s))} \mid s \in S^\flat \}$$

and if $\varepsilon(S) \in \bigotimes_{\alpha \in J} \mathcal{S}_\alpha$, then $((e_\varepsilon)_{S \times \varepsilon(S)}, (E_\varepsilon)_{S \times \varepsilon(S)})$ is surjective.

Theorem 2.5 Let ε be the point evaluation function induced by $\mathbf{BC}_{\mathbf{fPDitop}}(S, S_\alpha) = \{ \psi_\alpha \mid \alpha \in A \}$. Then $(e_\varepsilon, E_\varepsilon)$ is the evaluation difunction induced by the family $\mathbf{BC}(S, S_\alpha) = \{ (f_{\psi_\alpha}, F_{\psi_\alpha}) \mid \alpha \in J \}$.

Proof We must show that $\pi_\alpha \circ e_\varepsilon = f_{\psi_\alpha}$ and $\Pi_\alpha \circ E_\varepsilon = F_{\psi_\alpha}$. Let $\pi_\alpha \circ e_\varepsilon \not\subseteq \overline{Q}_{(k, s_\alpha)}$ for some $k \in S$ and $s_\alpha \in S_\alpha$. Then there exists $r \in S$ and $w_\alpha \in S_\alpha$ such that $\overline{P}_{(r, w_\alpha)} \not\subseteq \overline{Q}_{(k, s_\alpha)}$ where $e_\varepsilon \not\subseteq \overline{Q}_{(r, (u_\alpha)_{\alpha \in J})}$ and $\pi_\alpha \not\subseteq \overline{Q}_{((u_\alpha)_{\alpha \in J}, w_\alpha)}$. However, $k = r$ and $P_{w_\alpha} \not\subseteq Q_{s_\alpha}$ and so $e_\varepsilon \not\subseteq \overline{Q}_{(k, (u_\alpha)_{\alpha \in J})}$. Since $\pi_\alpha \not\subseteq \overline{Q}_{((u_\alpha)_{\alpha \in J}, w_\alpha)}$, then $\overline{P}_{((v_\alpha)_{\alpha \in J}, v_\alpha)} \not\subseteq \overline{Q}_{(u_\alpha)_{\alpha \in J}, w_\alpha}$ for some $(v_\alpha)_{\alpha \in J} \in \prod_{\alpha \in J} S_\alpha$. Therefore, $(v_\alpha)_{\alpha \in J} = (u_\alpha)_{\alpha \in J}$ and $P_{u_\alpha} \not\subseteq Q_{w_\alpha}$. By definition of e_ε , we may write $\overline{P}_{(s', \varepsilon(s'))} \not\subseteq \overline{Q}_{(k, (u_\alpha)_{\alpha \in J})}$ for some $s' \in S$. Then we have $P_{\varepsilon(k)} \not\subseteq Q_{(u_\alpha)_{\alpha \in J}}$, that is $P_{(\psi_\alpha(k))_{\alpha \in J}} \not\subseteq Q_{(u_\alpha)_{\alpha \in J}}$ and by [5, Corollary 1.4] $P_{\psi_\alpha(k)} \not\subseteq Q_{u_\alpha}$ for all $\alpha \in J$. Since $P_{w_\alpha} \not\subseteq Q_{s_\alpha}$ and $P_{u_\alpha} \not\subseteq Q_{w_\alpha}$ then $Q_{s_\alpha} \subseteq Q_{u_\alpha}$. This gives that $P_{\psi_\alpha(k)} \not\subseteq Q_{s_\alpha}$, that is $f_{\psi_\alpha} \not\subseteq \overline{Q}_{(k, s_\alpha)}$. As a result $\pi_\alpha \circ e_\varepsilon \subseteq f_{\psi_\alpha}$ and by [5, Proposition 2.27] we have $\Pi_\alpha \circ E_\varepsilon \subseteq F_{\psi_\alpha}$.

Now we show that $F_{\psi_\alpha} \subseteq \Pi_\alpha \circ E_\varepsilon$. Let $F_{\psi_\alpha} \not\subseteq \overline{Q}_{(k, s_\alpha)}$ and $\overline{P}_{(k, s_\alpha)} \not\subseteq \Pi_\alpha \circ E_\varepsilon$ for some $k \in S, s_\alpha \in S_\alpha$. By the definition of composition, $\overline{P}_{(k, s_\alpha)} \not\subseteq \overline{Q}_{(s, u_\alpha)}$ and $\overline{P}_{(s, (t_\alpha)_{\alpha \in J})} \not\subseteq E_\varepsilon, \overline{P}_{((t_\alpha)_{\alpha \in J}, u_\alpha)} \not\subseteq \Pi_\alpha$ where $s \in S, u_\alpha \in S_\alpha, (t_\alpha)_{\alpha \in J} \in \prod_{\alpha \in J} S_\alpha$. However, $s = k$ and $P_{s_\alpha} \not\subseteq Q_{u_\alpha}$ and so $\overline{P}_{(k, (t_\alpha)_{\alpha \in J})} \not\subseteq E_\varepsilon$. By the definition of Π_α , we may write $\overline{P}_{((t_\alpha)_{\alpha \in J}, u_\alpha)} \not\subseteq \overline{Q}_{((v_\alpha)_{\alpha \in J}, v_\alpha)}$ for some $(v_\alpha)_{\alpha \in J} \in \prod_{\alpha \in J} S_\alpha$. Therefore, $(t_\alpha)_{\alpha \in J} = (v_\alpha)_{\alpha \in J}$ and $P_{u_\alpha} \not\subseteq Q_{v_\alpha}$. By the definition of E_ε , we may write that $\overline{P}_{(k, (t_\alpha)_{\alpha \in J})} \not\subseteq \overline{Q}_{(s', \varepsilon(s'))}$ for some $s' \in S$. Then we have $P_{(t_\alpha)_{\alpha \in J}} \not\subseteq Q_{\varepsilon(k)}$, that is $P_{(t_\alpha)_{\alpha \in J}} \not\subseteq Q_{(\psi_\alpha(k))_{\alpha \in J}}$ and by [5, Corollary 1.4] $P_{t_\alpha} \not\subseteq Q_{\psi_\alpha(k)}$ for all $\alpha \in J$. Since $P_{s_\alpha} \not\subseteq Q_{u_\alpha}$ and $P_{u_\alpha} \not\subseteq Q_{t_\alpha}$ then $P_{t_\alpha} \subseteq P_{s_\alpha}$. This gives that $P_{s_\alpha} \not\subseteq Q_{\psi_\alpha(k)}$, that is $\overline{P}_{(k, s_\alpha)} \not\subseteq F_{\psi_\alpha}$. But this is a contradiction. As a result $F_{\psi_\alpha} \subseteq \Pi_\alpha \circ E_\varepsilon$ and by [5, Proposition 2.27] we have $f_{\psi_\alpha} \subseteq \pi_\alpha \circ e_\varepsilon$.

Now consider the family $\mathbf{BC}(S, \mathbb{I}) = \{ (f_\psi, F_\psi) \mid \psi \in \mathbf{BC}_{\mathbf{fPDitop}}(S, \mathbb{I}) \}$. Let $(e_\varepsilon, E_\varepsilon)$ be the evaluation difunction induced by $\mathbf{BC}(S, \mathbb{I})$.

Theorem 2.6 Let $\varepsilon(S) \in \bigotimes_{\alpha \in J} \mathcal{I}_\alpha$ and $(S, \mathcal{S}, \tau, \kappa)$ be a T_0 and completely biregular in $\mathbf{dfPDitop}$. Then there exists a dihomeomorphic embedding from S to the Tychonoff dicube. $[\varepsilon(S)]$ is called the Stone–Céché compactification of S .

Proof By Theorem 1.4, $(S, \mathcal{S}, \tau, \kappa)$ is also completely biregular in **fPDitop**. By Theorem 1.5, $(e_\varepsilon, E_\varepsilon)$ is injective and bicontinuous. Further, by Corollary 2.4, $((e_\varepsilon)_{(S \times B)}, (E_\varepsilon)_{(S \times B)})$ is surjective where $B = e_\varepsilon^{-1}S$. Now we show that it is open. Let $G \in \tau$ and $G \not\subseteq Q_s$. Since **BC**(S, \mathbb{I}) separates q-sets and open sets, we have $f_\psi^{-1}P_s \subseteq]F_\psi^{-1}G[$ for some $\psi \in \mathbf{BC}_{\mathbf{fPDitop}}(S, \mathbb{I})$. Since the projection difunction (π_α, Π_α) is bicontinuous, then $\pi_\psi^{-1}]F_\psi^{-1}G[$ is open in S and

$$(e_\varepsilon)_{(S \times B)}^{-1}P_s = e_\varepsilon^{-1}P_s \subseteq (\pi_\psi^{-1} \circ \pi_\psi)(e_\varepsilon^{-1}P_s) = \pi_\psi^{-1}(\pi_\psi \circ e_\varepsilon)^{-1}P_s = \pi_\psi^{-1}f_\psi^{-1}P_s \subseteq \pi_\psi^{-1}]F_\psi^{-1}G[.$$

Therefore, we find $(e_\varepsilon)_{(S \times B)}^{-1}G \subseteq \pi_\psi^{-1}]F_\psi^{-1}G[$. Further,

$$\pi_\psi^{-1}]F_\psi^{-1}G[\subseteq \pi_\psi^{-1}F_\psi^{-1}G = \pi_\psi^{-1}(\Pi_\psi \circ E)^{-1}G = (\pi_\psi^{-1} \circ \Pi_\psi)^{-1}(E_\varepsilon^{-1}G) \subseteq E_\varepsilon^{-1}G = (E_\varepsilon)_{(S \times B)}^{-1}G$$

As a result,

$$(e_\varepsilon)_{(S \times B)}^{-1}G \subseteq \pi_\psi^{-1}]F_\psi^{-1}G[\subseteq (E_\varepsilon)_{(S \times B)}^{-1}G$$

However, since $((e_\varepsilon)_{(S \times B)}^{-1}, (E_\varepsilon)_{(S \times B)})$ is bijective, by [5, Corollary 2.33.(1)(i)], we find

$$(e_\varepsilon)_{(S \times B)}^{-1}G = \pi_\psi^{-1}]F_\psi^{-1}G[= (E_\varepsilon)_{(S \times B)}^{-1}G$$

Now let $P_s \not\subseteq K$ and $K \in \kappa$. Since **BC**(S, \mathbb{I}) separates p-sets and closed sets, we have $F_\psi^{-1}Q_s \supseteq]f_\psi^{-1}K[$ for some $\psi \in \mathbf{BC}_{\mathbf{fPDitop}}(S, \mathbb{I})$. In this case,

$$E_\varepsilon^{-1}Q_s = (\Pi_\psi^{-1} \circ \Pi_\psi)^{-1}E^{-1}Q_s = \Pi_\psi^{-1}F_\psi^{-1}Q_s \supseteq \Pi_\psi^{-1}]f_\psi^{-1}K[,$$

that is

$$(E_\varepsilon)_{(S \times B)}^{-1}K = E^{-1}K = E^{-1} \bigcap \{Q_s \mid P_s \not\subseteq K\} = \bigcap \{E^{-1}Q_s \mid P_s \not\subseteq K\} \supseteq \Pi_\psi^{-1}]f_\psi^{-1}K[.$$

Further,

$$(e_\varepsilon)_{(S \times B)}^{-1}K = e_\varepsilon^{-1}K \subseteq (\pi_\psi^{-1} \circ \pi_\psi)^{-1}(e_\varepsilon^{-1}K) \subseteq \pi_\psi^{-1}(\pi_\psi \circ e_\varepsilon)^{-1}K = \pi_\psi^{-1}f_\psi^{-1}K \subseteq \Pi_\psi^{-1}]f_\psi^{-1}K[.$$

As a result, we find

$$e_\varepsilon^{-1}K \subseteq \Pi_\psi^{-1}]f_\psi^{-1}K[\subseteq E^{-1}K.$$

Since $((e_\varepsilon)_{(S \times B)}^{-1}, (E_\varepsilon)_{(S \times e_\varepsilon^{-1}S)})$ is bijective, by [5, Corollary 2.33.(1)(i)], we find

$$(e_\varepsilon)_{(S \times B)}^{-1}K = \Pi_\psi^{-1}]f_\psi^{-1}K[= (E_\varepsilon)_{(S \times B)}^{-1}K.$$

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Received: September 17, 2007